Special Theory of Relativity







Measurement of Time in STR



$$\Delta t_o = \Delta t_P \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

Where, v is the Relative Speed of the Two Frames $\Delta t_{O} \rangle \Delta t_{P}$

Time interval w. r. t the stationary frame Time interval w. r. t the moving frame

This is called Time Dilation !

Measurement of Length in STR



$$l^1 = l \sqrt{1 - \frac{v^2}{c^2}}$$

This equation is called relativistic length equation!

If $v > 0 \implies \frac{v}{-1} < 1$





 l^1

$$l^{1} = l \ (< 1)$$

< l

This is called Length Contraction ! Length measured by an observer in the car Length measured by observer on the Earth

Doppler's Effect in STR

If a light source in uniform motion approaches or recedes a stationary observer then the frequency of light is observed to change. This is known as **Doppler effect** in STR.



This is the general form of the Doppler's Effect in STR!



A yellow coloured vehicle appears as a green coloured vehicle to a stationary observer due to its speed. Find the velocity of the vehicle. (Wavelengths of yellow and green light are 550nm and 500nm respectively)

Is the above incident practically possible??? Briefly explain your answer.

Source frequency = true colour of the vehicle f_s = frequency of the yellow colour

For E-M Waves : $v = f \lambda$ $f = \frac{c}{\lambda}$ $f_s = \frac{3 \times 10^8 \, m s^{-1}}{550 \times 10^{-9} \, m}$ $f_s = 5.45 \times 10^{14} \, Hz$



Then, the frequency appears to increase! That means, the car is directly approaching to the observer! :. Using the Doppler's equation,



$$f_{o} = f_{s} \sqrt{\frac{1+\beta}{1-\beta}} \implies 6.00 \times 10^{14} = 5.45 \times 10^{14} \sqrt{\frac{1+\beta}{1-\beta}}$$
$$1.1 = \sqrt{\frac{1+\beta}{1-\beta}} \implies 1.21 = \frac{1+\beta}{1-\beta}$$
$$\beta = \frac{0.21}{2.21} \implies \frac{v}{c} = \frac{0.21}{2.21} \implies \frac{v}{c} = 0.095 \implies v = 0.095c$$
$$v = 2.8 \times 10^{7} m s^{-1}$$

This is a practically impossible velocity !

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The mass – energy equivalence

In Physics, mass – energy equivalence is the concept that the mass of a body is a measure of its energy content.

Albert Einstein proposed mass – energy equivalence in 1905. The equivalence is described by the famous equation,



The equation $\mathbf{E} = \mathbf{m} \mathbf{c}^2$ indicates that energy always exhibits mass in whatever from the energy takes. It does not imply that mass may be "**converted**" to energy, for modern theory holds that neither mass or energy may be destroyed, but only moved from one location to another.

Proof of E = m c^2 [Einstein's Box]

This is a Hypothetical Experiment.

Before Einstein, it was known that a beam of light pushes against matter; that is known as Radiation Pressure. This means the light has momentum, E/c. Einstein used this fact to show that radiation (light) energy has an equivalent mass.

Consider a cylinder of mass M. A pulse of light with energy E is emitted from the left side. The cylinder recoils to the left with velocity V. If the mass of cylinder is large, it doesn't move far before the light reaches the



other side. So, the light must travel a distance L, requiring time t = L/c. In this time, the cylinder travels a distance x.



Momentum of the photon give the momentum to the cylinder.

Momentum of the photon =

Momentum of the Box

$$\frac{E}{c} = M V$$

01

Time for light beam to cross the cylinder = $\begin{bmatrix} L \\ t \end{bmatrix}$

Distance traveled by the cylinder = x = V t

P.T.O

03

02



Einstein was not the first to propose a mass-energy relationship. However, Einstein was the first scientist to propose the $\mathbf{E} = \mathbf{m} \mathbf{c}^2$ formula and the first to interpret mass-energy equivalence as a fundamental principle that follows from the relativistic symmetries of Space & Time!

The mass – energy equivalence



4-meter-tall sculpture of <u>Einstein</u>'s 1905 $E = mc^2$ formula at the 2006 <u>Walk</u> <u>of Ideas, Berlin, Germany</u>.

Find the mass-equivalence energy of a 1kg.
Using,
$$E = mc^2$$

 $E = (1) (3 \times 10^8)^2$
 $E = 9 \times 10^{16} J$

This is a very large energy. Using this energy, we can vaporize $\sim 10^{10} \text{ kg}$ of water at the room temperature $(30^{\circ}\text{C})!$ $\therefore E = ms\theta + mL$

Equivalence of mass and energy





Einstein put forward new ideas regarding the relationship between space, time, mass and energy which have come to be known as the theory of relativity. It had long been accepted that matter could not be destroyed. This assumption was expressed in the *law of conservation of matter*, which states that the total quantity of matter in the universe is fixed and cannot be increased or decreased by human agency.

Twin Paradox



